# SHIVAJI UNIVERSITY, KOLHAPUR



Established: 1962

 $A^{\rm ++}$  Accredited by NAAC (2021) with CGPA 3.52

Structure and Syllabus in Accordance with

**National Education Policy - 2020** 

with Multiple Entry and Multiple Exit

of

Master of Science (Applied Statistics and Informatics)

under Faculty of Science and Technology

(To Be Implemented From Academic Year 2023-24)

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#### 1. Preamble

The M.Sc. (Applied Statistics and Informatics) programme at Shivaji University, Kolhapur, is a dynamic postgraduate programme designed to provide students with a comprehensive knowledge of statistical methods and their applications in the realm of informatics. This programme merges statistical analysis with information technology, enabling students to extract valuable insights from complex data sets. Through a blend of theoretical teachings and practical hands-on experience, students acquire proficiency in data analysis, visualization, and interpretation. The curriculum emphasizes real-world problem-solving and equips graduates with the skills to make informed decisions in diverse sectors such as business, healthcare, and technology, where data-driven strategies are pivotal.

#### 2. Duration

• 2 Years

#### **3. Eligibility for Admission**

• Three-year B. Sc. Degree with Statistics as principal / major subject

#### 4. Medium of Instruction

• English

## 5. Programme Structure

## Structure in Accordance with National Education Policy - 2020 With Multiple Entry and Multiple Exit Options M.Sc. (Applied Statistics and Informatics) Part – I (Level - 6.0)

	Course Code Teaching Scheme				Examination Scheme					
			ry and Practi		University Assessment (UA)		Internal Assessment (IA)			
		Lectures +	Practical	Credit	Maximum	Minimum	Exam. Hours	Maximum	Minimum	Exam.
		Tutorial/	(Hours/		Marks	Marks		Marks	Marks	Hours
		(Hours/	week)							
		week)			Semester-I					
	MMT11	4		4	80	32	3	20	8	0.5
Major	MMT12	4		4	80	32	3	20	8	0.5
Mandatory	MMT13	2		2	40	16	1.5	10	4	0.25
	MMP14		12	4				100	40	3
Major Elective	MET1	4		4	80	32	3	20	8	0.5
Research Methodology	RM	4		4	80	32	3	20	8	0.5
Tot	tal			22	360			190		
					Semester-II					
	MMT21	4		4	80	32	3	20	8	0.5
Major	MMT22	4		4	80	32	3	20	8	0.5
Mandatory	MMT23	2	-	2	40	16	1.5	10	4	0.25
_	MMP24		12	4				100	40	3
Major Elective	MET2	4		4	80	32	3	20	8	0.5
OJT/FP	OJT/FP	4		4			*			
Tot				22						
Total (Sem I +	Sem II)			44						

MMT–Major Mandatory Theory	• Total Marks for M.ScI : 1100						
MMP–Major Mandatory Practical	• Total Credits for M.ScI (Semester I & II) : 44						
MET–Major Elective Theory	Separate passing is mandatory for University and Internal						
RM - Research Methodology Examinations							
• OJT/FP- On Job Training/ Field Project							
* Evaluation scheme for OJT/FP shall be decided by concerned BOS							
Requirement for Entry at Level 6.0: B. Sc. degree of 3 years with Statistics as Principle/Major Subject.							
• Requirement for Exit after Level 6.0:							
Student can exit after completion of Level 6.0 with Post Graduate Diploma in Applied Statistics and Informatics							
• Requirement for Entry at Level 6.5: Completion of Level 6.0 with Statistics as Principle/Major Subject.							

## Structure in Accordance with National Education Policy - 2020 With Multiple Entry and Multiple Exit Options M.Sc. (Applied Statistics and Informatics) Part – II (Level-6.5)

	Course Code	Teaching Scheme			Examination Scheme						
			ry and Practi			University Assessment (UA)			Internal Assessment (IA)		
		Lectures + Tutorial/ (Hours/ week)	Practical (Hours/ week)	Credit	Maximum Marks	Minimum Marks	Exam. Hours	Maximum Marks	Minimum Marks	Exam. Hours	
					Semester-III						
	MMT31	4		4	80	32	3	20	8	0.5	
Major	MMT32	4		4	80	32	3	20	8	0.5	
Mandatory	MMT33	2	-	2	40	16	1.5	10	4	0.25	
	MMP34		12	4				100	40	3	
Major Elective	MET3	4		4	80	32	3	20	8	0.5	
Research Project	RP			4			#				
Tot	al			22							
					Semester-IV				-		
	MMT41	4		4	80	32	3	20	8	0.5	
Major Mandatory	MMT42	4		4	80	32	3	20	8	0.5	
	MMP43		12	4				100	40	3	
Major Elective	MET4	4		4	80	32	3	20	8	0.5	
Research Project	RP			6	6 ##						
Tot	al			22							
Total (Sem I +	Sem II)			44							

MMT–Major Mandatory Theory	• Total Marks for M.ScII : 1100					
MMP–Major Mandatory Practical	• Total Credits for M.ScII (Semester III & IV) : 44					
MET–Major Elective	• Separate passing is mandatory for University and Internal					
RP- Research Project	Examinations					
# Evaluation scheme for Research Project shall be decided by concerned BOS						
## Evaluation scheme for Research Project shall be decided by concerned BOS						

## 6. Programme Outcomes (POs) and Programme Specific Outcomes (PSOs)

## **Programme Outcomes (POs)**

Post Graduates of the M.Sc. Applied Statistics and Informatics programme will be able to:

- Have sufficient knowledge of theoretical concepts in Statistics for (i) choosing and applying the most appropriate statistical methods/ techniques for collecting and analyzing data (ii) interpreting the results of analyses in relation to given real life situations.
- Have ability to explain the inter-connections between various sub disciplines and apt use of these inter-connections in modelling real life problems.
- Have ability to recognize the importance of statistical thinking and training, and to acquire the state-of-the-art developments in Statistics independently from available resources.
- Develop expertise in statistical research and real life data analysis.

## **Programme Specific Outcomes (PSOs)**

After completion of M.Sc. Applied Statistics and Informatics programme the student will be able to:

- Develop stochastic models for studying, analyzing, interpreting and forecasting real life phenomenon in diverse disciplines.
- Effectively use necessary statistical software and computing environment including C, C++, R, Python, MS-EXCEL among others and have expertise in handling computational systems for data storage, update and retrieval.
- Have the versatility to work effectively in a broad range of establishments (including R&D sectors, analytics, scientific laboratories, government, financial, health, educational) or to continue for higher education, and exhibit ethical and professional behaviour in team work.

## 7. Course Codes

Semester-I									
Sr. No.	Major Mandatory								
1	Distribution Theory	MSU0325MML905G1							
2	Estimation Theory	MSU0325MML905G2							
3	Statistical Computing	MSU0325MML905G3							
4	Practical I	MSU0325MMP905G4							
5	Research Methodology in Statistics	MSU0325RML905G							
	Major Elective								
	Fundamentals of Computer	MSU0325MEL905G1							
6	Programming								
	Statistical Programming using C	MSU0325MEL905G2							
	Semester-II								
Sr. No.	Major Mandato	ry							
1	Theory of Testing of Hypothesis	MSU0325MML905H1							
2	Linear Models and Regression Analysis	MSU0325MML905H2							
3	Statistical Programming using Python	MSU0325MML905H3							
4	Practical-II	MSU0325MMP905H4							
5	On Job Training/Field Project	MSU0325OJP905H/							
5		MSU0325FPP905H							
Major Elective									
	Advanced Data Structure with C++	MSU0325MEL905H1							
6	Cloud computing and Data Visualization	MSU0325MEL905H2							
U	Statistical Programming using C++	MSU0325MEL905H3							
	Reliability Theory	MSU0325MEL937H4							

#### M. Sc. Applied Statistics and Informatics (Part I) (Level-6.0) (Semester I) (NEP-2020) (Introduced from Academic Year 2023-24)

#### **Title of Course:** DISTRIBUTION THEORY **Course Code:** MSU0325MML905G1 **Total Credits:** 04 **Course outcomes:**

Upon successful completion of this course, the students will be able to:

- i) Understand and explain the concept of univatiate and multivariate random variables and related entities
- ii) Understand and explain the nature of various probability distributions and perform related computations.
- iii) Understand probability models for multivariate data and perform related computations
- iv) Understand non-central sampling distribution and able to perform their applications, able to perform computations related to order statistics

Unit 1: Random variable, Cumulative distribution function (CDF) and its properties, continuous and discrete distributions, mixtures of probability distributions, decomposition of mixture CDF into discrete and continuous CDFs, computation of probabilities of events using CDF, expectation and variance of mixture distributions. Quantiles of probability distributions. Transformations of univariate random variables, probability integral transformation. (12L+3T)

**Unit 2:** Concepts of location, scale and shape parameters of distributions with examples. Symmetric distributions and their properties. Moment inequalities: Basic, Holder, Markov, Minkowski, Jensen, Chebyshev's inequalities, and their applications. Random vectors, joint distributions, Independence, variance-covariance matrix, joint MGF. Conditional expectation and variances. Transformations of bivariate random variables, Convolutions, compound distributions. (12L+3T)

**Unit 3:** Multivariate normal distribution, two definitions and their equivalence, singular and nonsingular normal distribution, characteristic function, moments, marginal and conditional distributions. Maximum likelihood estimators of the parameters of the multivariate normal distribution and their sampling distributions. Wishart matrix and its distribution (statement only), properties of Wishart distribution, distribution of generalized variance(statement only). Marshall-Olkin bivariate exponential distributions. (12L+3T)

**Unit 4:** Non-central chi-square, t and F distributions, distributions of linear and quadratic forms involving normal random variables, Fisher Cochran and related theorems (statements only) and their applications. Order Statistics: Distribution of an order statistics, joint distributions of two order statistics, distribution of spacings, normalized spacings with illustration to exponential case, distribution of sample median and sample range. (12L+3T) **References:** 

- 1. Casella, G., & Berger, R. L. (2021). Statistical inference. Cengage Learning.
- 2. DasGupta, A. (2010). Fundamentals of probability: A first course. Springer Science & Business Media.
- 3. Johnson N. L. & Kotz. S. (1996). Distributions in Statistics Vol-I, II and III. JohnWiley and Sons New York.
- 4. Kotz, S., Balakrishnan, N., & Johnson, N. L. (2004). Continuous multivariate distributions, Volume 1: Models and applications (Vol. 1). John Wiley & Sons.
- 5. Rao C. R. (1995). Linear Statistical Inference and Its Applications. John Wiley & Sons.
- 6. Rohatagi V. K. & Saleh A. K. Md. E.(2001). Introduction to Probability Theory and Mathematical Statistics. John Wiley and sons Inc.

#### **Title of Course:** ESTIMATION THEORY **Course Code:** MSU0325MML905G2 **Total Credits:** 04 **Course outcomes:**

Upon successful completion of this course, the students will be able to:

- i) Explain the principles of data reduction and obtain sufficient, minimal sufficient, and complete statistics for various families of distributions.
- ii) Obtain UMVUE of parameters of various distributions and determine Cramer-Rao and Chapman-Robbins-Kiefer lower bounds for the variances of unbiased estimators.
- iii) Apply parametric and nonparametric methods to obtain estimators.
- iv) Obtain CAN and BAN estimators.

**Unit 1:** Principles of data reduction: sufficiency principle; sufficient statistics; factorization theorem; minimal sufficient statistic; minimal sufficient statistic for exponential family, power series family, curved exponential family, and Pitman family; completeness; bounded completeness; ancillary statistics, Basu's theorem and it's applications.

(12L + 3T)

**Unit 2:** Unbiased estimation: unbiased estimator; uniformly minimum variance unbiased estimator (UMVUE); A necessary and sufficient condition for an estimator to be UMVUE; Rao-Blackwell theorem and Lehmann-Scheffe theorem, and their applications in finding UMVUEs; Fisher information function and Fisher information matrix; Cramer-Rao lower bound; Chapman-Robbins-Kiefer lower bound.

(12L + 3T)

**Unit 3:** Methods of finding estimators: method of moments estimator; maximum likelihood estimator (MLE), properties of MLE, MLE in nonregular families; method of scoring; method of minimum chi-square, EM algorithm. Nonparametric estimation: degree of an estimable parameter, kernel, U-statistic and its properties.

(12L + 3T)

**Unit 4**: Consistency of an estimator, weak and strong consistency, joint and marginal consistency, invariance property under continuous transformations, methods of constructing consistent estimators, Comparison of consistent estimators, asymptotic relative efficiency, minimum sample size required by the estimator to attain certain level of accuracy. Consistent Asymptotic Normal (CAN) Estimators: Definition of CAN estimator for real and vector valued parameters, invariance of CAN property under non-vanishing differentiable transformation (delta method). Methods of constructing CAN estimators: Method of Moments, method of percentiles, comparison of CAN estimators. BAN estimators, CAN and BAN estimators in one parameter and multi-parameter exponential family of distributions, Crammer family of distributions, Cramme

$$(12L + 3T)$$

- 1. Casella, G., & Berger, R. L. (2021). Statistical inference. Cengage Learning.
- 2. Deshmukh S., Kulkarni M. (2022). Asymptotic Statistical Inference: A Basic Course Using R. Springer Verlag, Singapor.
- 3. Dudewicz, E. J., & Mishra, S. (1988). Modern mathematical statistics. John Wiley & Sons, Inc.
- 4. Kale, B. K., & Muralidharan, K. (2015). Parametric inference: An introduction. Alpha Science International Limited.
- 5. Lehmann, E. L. (1983). Theory of Point Estimation. John Wiley & sons.
- 6. Mukhopadhyay, P. (2015). Mathematical Statistics, Books and Allied (p) Ltd.
- 7. Rao C. R. (1995). Linear Statistical Inference and Its Applications. John Wiley & Sons.
- 8. Rohatgi, V. K., & Saleh, A. M. E. (2015). An introduction to probability and statistics. John Wiley & Sons.

#### **Title of Course:** STATISTICAL COMPUTING **Course Code:** MSU0325MML905G3 **Total Credits:** 02 **Course outcomes:**

Upon successful completion of this course, the students will be able to:

- i) Perform data organization, data manipulation, statistical and mathematical computations, and data analysis using MSEXCEL.
- ii) Perform data organization, data manipulation, statistical and mathematical computations, and data analysis using R.

**Unit 1:** MSEXCEL: Introduction to MSEXCEL. Cell formatting, conditional formatting, Data manipulation using EXCEL: sort and filter, find and replace, text to columns, remove duplicate, data validation, consolidate, what-if-analysis. Working with Multiple Worksheets and Workbooks. Built-in mathematical and statistical functions for obtaining descriptive statistic, computing PMF/PDF, CDF and quantiles of the well-known distributions, rand and randbetween function, Logical functions: if, and, or, not. Lookup functions: hlookup, vlookup, Formula Errors, Creating and Working with Charts, Database functions, Text functions, Date and time functions, Excel add-ins: analysis tool pack, Pivot tables and charts.

(12L+3T)

**Unit 2:** R-software: Introduction to R, data types and objects, operators, data input, data import and export, built in functions for descriptive statistics, random sampling and computation of pdf, cdf and quantiles of well known distribution. Strings and Dates in R. apply family of functions. Saving work in R. Matrix algebra, graphical procedures, frequencies and cross tabulation, built in functions: lm, t.test, prop.test, wilcox.test, ks.test, var.test, chisq.test, aov. Control statements. Programming, user defined functions, R- packages. R-studio.

(12L+3T)

- 1. Gardener, M. (2012). Beginning R: the statistical programming language. John Wiley & Sons.
- 2. Held, B., Moriarty, B., & Richardson, T. (2019). Microsoft Excel Functions and Formulas with Excel 2019/Office 365. Mercury Learning and Information.
- 3. Herkenhoff, L., & Fogli, J. (2013). Applied statistics for business and management using Microsoft Excel. New York: Springer.
- 4. Purohit, S. G., Gore, S. D., & Deshmukh, S. R. (2015). Statistics using R. Alpha Science International.
- 5. Thulin, M. (2021). Modern Statistics with R: From wrangling and exploring data to inference and predictive modelling. BoD-Books on Demand.
- 6. Weblinks: <u>https://support.microsoft.com/en-us/excel</u> <u>https://cran.r-project.org/manuals.html</u>

# **Title of Course:** FUNDAMENTALS OF COMPUTER PROGRAMMING **Course Code:** MSU0325MEL905G1

#### Total Credits: 04

#### **Course outcomes:**

Upon successful completion of this course, the students will able to:

- i) Develop algorithms, flowcharts for simple as well as complex algorithms.
- ii) Describe how data represented, manipulated, and stored in a computer.
- iii) Understand and apply the control structures while writing program.
- iv) Understand and use an arrays, pointers and structures effectively in programming.

**Unit 1:** Overview of Computer programming, Algorithms: The concept and features of the algorithm, ways of writing the algorithm, writing step by step procedure, Problem redefinition, Flow charts/Decision Trees: various symbols used to develop a flow chart, Advantages and drawbacks of flowcharts, concept of Tracing and Testing of Algorithm/flowchart. Pseudo code generation. Fundamentals of C programming: Features of C language, structure of C program, comments, header files, data types, constants and variables, operators, expressions, evaluation of expressions, type conversion, precedence and associativety, I/O functions.

(12 L + 3 T)

**Unit 2:** Control Structures: Decision control structures and Loop control structures. Structured programming, Modular programming, TOP DOWN/BOTTAM UP approach, Recursive algorithms, Examples, Illustrating structured program development methodology and use of block structured algorithmic language to solve specific problem. Syntax and semantics, documentation and debugging of a program.

(12 L + 3 T)**Unit 3:** Advanced Data Types and their implementation: Arrays, Strings, Records, Pointers, Structures, Union, and Applications in the record keeping of real life system. Dynamic memory allocation using MALLOC, CALLOC and REALLOC.

(12 L + 3 T)

(12 L + 3 T)

**Unit 4:** Searching, Sorting and Update of the data: Various methods, Design and Analysis of algorithms - Devide and conqure, Backtracking. Dynamic programming, Emphasis should be given on better programming styles and implementation is expected through C compiler.

- 1. Balagurusamy, E. (2016). Programming In Ansi C.
- 2. Horowitz & Sahani (1998). Fundamentals of Computer Algorithms. GalgotiaPublications,
- 3. Knuth D. E. (1997). *The Art of Computer Programming*. Volume 1: Fundamental -Narosa Publishing House.
- 4. Kruse R. L. (2006): *Data structures and program design C*, 2nd edition-PEARSON.
- 5. Ravichandran D. *Programming with C++*, 3rd edition, McGraw Hill Education.
- 6. Shukla R. K. (2015). Analysis and Design of Algorithms, A beginners approach. Wiley.

#### **Title of Course:** STATISTICAL PROGRAMMING USING C **Course Code:** MSU0325MEL905G2 **Total Credits:** 04

#### **Course outcomes:**

Upon successful completion of this course, the students will able to:

- i) Understand the C programming.
- ii) Describe how data represented, manipulated, and stored in a computer.
- iii) Understand and apply the control structures while writing program.
- iv) Understand and use an arrays, pointers and structures effectively in programming.

**Unit 1:** Overview of C: History and importance of C, Basic structure of C program, executing a simple C program. Constants, Variable and Data Types: Introduction, Character Set, C Tokens, Keywords and Identifiers, Constants, Variables, Data Types, Declaration of Variables, Assigning Values to Variables, Defining Symbolic Constants. Managing Input and Output Operations: Reading a Character, Writing a Character, Formatted Input, Formatted Output. Operators and Expressions: Introduction, Arithmetic Operators, Relational Operators, Logical Operators, Assignment Operators, Increment and Decrement Operators, Conditional Operator, Bitwise Operators, Special Operators, Arithmetic Expressions, Evaluation of Expressions, Precedence of Arithmetic Operators, Type Conversions in Expressions, Operator Precedence and Associativity.

(12 L + 3 T)

**Unit 2:** Decision Making and Branching: Introduction, Decision Making with IF Statement, Simple IF Statement, the IF-ELSE Statement, Nesting of IF-ELSE Statements, The ELSE IF Ladder, The Switch statement, The '? :' Operator, The goto statement. Decision Making and Looping: Introduction, the while statement, the do-while statement, the for statement, continue and break statement. User-defined Functions: Need for functions, Elements of User-defined Functions, Definition of Functions, Return Values and their Types, Function Calls, Function Declaration, Category of Functions, No Arguments and no Return Values, Arguments but no Return values, Arguments with Return Values, No Arguments but Returns a Value Recursion, The Scope, Visibility and Lifetime of variables.

(12 L + 3 T)

**Unit 3:** Arrays: One-dimensional Arrays, Declaration of One-dimensional Arrays, Initialization of One-dimensional Arrays, Two-dimensional Arrays, Declaration of Two-dimensional Arrays, Initialization of Two-dimensional Arrays, Array and functions, Passing Arrays to Functions, Character Arrays and Strings: Declaring and Initializing String Variables, Reading Strings from Terminal, Writing Strings to Screen, Arithmetic Operations on Characters, String-handling Functions, Example Programs (with and without using built-in string functions)

(12 L + 3 T)

(12 L + 3 T)

**Unit 4:** Pointers: Introduction, Declaring Pointer Variables, Initialization of Pointer variables, accessing a Variable through its Pointer, Pointer Expressions, Pointer Increments and Scale Factor. Structures: Introduction, Defining a structure, declaring structure variables, accessing structure members, structure initialization, array of structures. File Management in C: Introduction, Defining and opening a file, closing a file, Input/output and Error Handling on Files.

- 1. Dr. Guruprasad Nagraj, "C Programming for Problem Solving", Himalaya Publishing House. ISBN-978-93-5299-361-1.
- 2. E. Balaguruswamy, "Programming in ANSI C", 8th Edition, 2019, McGraw Hill Education, ISBN: 978-93-5316-513-0.
- 3. Jacqueline A Jones and Keith Harrow, "Problem Solving with C", Pearson Education. ISBN: 978-93-325-3800-9.
- 4. Kernighan B.W and Dennis M. Ritchie, "The C Programming Language", 2nd Edition, 2015, Pearson Education India, ISBN: 978-93-3254-944-9.
- 5. Pradip Dey, Manas Ghosh, "Programming in C", 2nd Edition, 2018, Oxford University Press, ISBN: 978-01-9949-147-6.
- 6. Yashavant P. Kanetkar, "Let Us C", 16th Edition, 2019, BPB Publications, ISBN: 978-93-8728-449-4.

### **Title of Course:** RESEARCH METHODOLOGY IN STATISTICS **Course Code:** MSU0325RML905G **Total Credits:** 04 **Course outcomes:**

Upon successful completion of this course, the students will be able to:

- i) Understand the concept of research, research process, and research ethics.
- ii) Understand and apply various sampling methods for data collection and estimate the parameters.
- iii) Understand the concept of simulation and able to simulate real life processes
- iv) Estimate bias and standard error of an estimator using resampling techniques, apply, numerical methods to solve systems of linear equations, to obtain the roots of a nonlinear equation, and to solve definite integrals.

**Unit 1:** Meaning of research, objectives of research, motivation in research, types of research, research approaches, significance of research, research methods vs. methodology, research and Scientific method, research process, criteria of good research, defining research problem, research design, Research Ethics, publication of research, Plagiarism, Intellectual property rights, Patents and its filing procedures. (12L+3T)

**Unit 2**: Sampling techniques: review of simple random sampling stratified random sampling, systematic random sampling, cluster sampling, two phase sampling, ratio and regression method of estimation. Probability proportional to size sampling: Cumulative total method, Lahiri's method, Hansen-Horwitz estimator and its properties, Horwitz-Thompson estimator, Des Raj estimators for a general sample size. Non-sampling errors, techniques for handling non-response: Hansen–Horwitz and Demings model for the effect of call-backs. Randomised response techniques, dichotomous population, Warners model, MLE in Warners model, unrelated question model. (12L+3T)

**Unit 3:** Concept and need of simulation, random number generator, true random number and pseudo random number generators, requisites of a good random number generator. Tests for randomness. Congruential method of generating uniform random numbers. Algorithms for generating random numbers from well-known univariate discrete and continuous distributions, generating random vectors from multinomial, bivariate normal, and bivariate exponential distributions, generating random numbers from mixture of distributions (related results without proofs). Acceptance-Rejection Technique. Use of random numbers to evaluate integrals, to study the systems involving random variables, to estimate event probabilities and to find expected value of random variables. Use of random numbers for generation and statistical tests. (12L+3T)

Unit 4: Resampling methods: Bootstrap methods, estimation of bias and standard errors, estimation of sampling distribution, confidence intervals. Jackknife method: estimation of bias and standard errors, bias reduction method. Numerical methods for solution to system of linear equations: Jacobi and Gauss-Seidel methods with convergence analysis. Numerical methods for finding roots of nonlinear equation: Newton-Raphson method, bisection method; Newton-Raphson for system of non- linear equations. Numerical integration: quadrature formula, trapezoidal rule and Simpson's rules for single integral. (12L+3T) **References:** 

- 1. Atkinson, K. E. (1989). An introduction to numerical analysis, John Wiley and Sons.
- 2. Chaudhuri, A., & Stenger, H. (2005). Survey sampling: theory and methods. CRC Press.
- 3. Cochran, W. G. (1977). Sampling techniques. John Wiley & Sons.
- 4. Devroye L. (1986). Non- Uniform Random Variate Generation. Springer- Verlag New York.
- 5. Efron, B., & Tibshirani, R. J. (1994). An introduction to the bootstrap. CRC press.
- 6. Kennedy, W. J., & Gentle, J. E. (2021). Statistical computing. Routledge.
- 7. Kothari, C. R. (2004). Research methodology: Methods and techniques. New Age International.
- 8. Morgan, B. J. (1984). Elements of simulation (Vol. 4). CRC Press.

- 9. Mukhopadhyay, P. (2008). Theory and methods of survey sampling. PHI Learning Pvt. Ltd..
- 10. Robert, C. P., Casella, G., & Casella, G. (1999). Monte Carlo statistical methods (Vol. 2). New York: Springer.
- 11. Ross, S. M. (2022). Simulation. Academic Press.
- 12. Rubinstein, R. Y., & Melamed, B. (1998). Modern simulation and modeling (Vol. 7). New York: Wiley.
- 13. Singh, D., & Chaudhary, F. S. (1986). Theory and analysis of sample survey designs. John Wiley & Sons.
- 14. Sukhatme P. V., Sukhatme S. & Ashok C (1984). Sampling Theory of surveys and applications . Iowa university press and Indian society of agricultural statistics, New Delhi.

## **Title of Course:** PRACTICAL-I **Course Code:** MSU0325MMP905G4 **Total Credits:** 04

#### **Course outcomes:**

Upon successful completion of this course, the student will be able to:

- 1. Sketching of various distribution functions and finding possible probability distribution to observed Data.
- 2. Compute UMVUE, MME and MLE using various methods.
- 3. Perform mathematical/statistical computations, statistical data analysis using built-in functions in MS-EXCEL and R and develop programs for various tasks.
- 4. Perform/Solve various statistical problems though simulation, numerical and re-sampling techniques.

#### **Practical List:**

- 1. Sketching of PDF/PMF and CDF
- 2. Fitting probability distribution and related inference.
- 3. Probability plots for various univariate probability distributions and their interpretations.
- 4. Applications of multivariate normal distribution.
- 5. UMVUE, MME and MLE
- 6. Methods of Scoring and method of minimum chi-square estimation
- 7. Estimation using EM Algorithm
- 8. Verification of consistency and CAN property of estimators.
- 9. Computations using MSEXCEL
- 10. Statistical analysis using MSEXCEL
- 11. Computations using R
- 12. R-Programming
- 13. Formulations of research problem and its design
- 14. Sampling techniques I
- 15. Sampling techniques II
- 16. Applications of Simulation techniques
- 17. Numerical Methods and Resampling Techniques
- 18-20. Based on elective course

#### M. Sc. Statistics (Part I) (Level-6.0) (Semester II) (NEP-2020) (Introduced from Academic Year 2023-24)

#### **Title of Course:** THEORY OF TESTING OF HYPOTHESES **Course Code:** MSU0325MML905H1 **Total Credits:** 04 **Course outcomes:**

Upon successful completion of this course, a student will be able to:

- i) Understand the concept of testing of hypothesis, test statistic, critical regions, size and power of a test.
- ii) Develop and apply MP test, UMPU test, similar tests and a test with Neyman structure.
- iii) Obtain and interpret different interval estimates of parameters.
- iv) Develop and apply large sample tests.

**Unit 1:** Problem of testing of hypothesis, null and alternative hypotheses, Simple and composite hypotheses, test function, Randomized and non-randomized tests, power function of a test, Most powerful (MP) test, Neyman-PearsonLemma, Monotone likelihood ratio property, Uniformly Most Powerful (UMP) test and its existence, determination of minimum sample size to achieve the desired strength of a test. Concept of p-value.

(12L+3T)

**Unit 2:** UMP tests for two sided alternatives, examples of their existence and non-existence. Unbiased test, Generalized Neyman Pearson lemma, UMPU tests and their existence in case of exponential families (Statements of the theorems only). Similar tests, test with Neyman structure. Tests for means of multivariate normal distributions based on Hotelling's  $T^2$  Statistic.

(12L+3T)

**Unit 3:** Interval estimation: Confidence interval, relation with testing of hypotheses problem, Uniformly Most Accurate(UMA) and Uniformly Most Accurate Unbiased(UMAU) confidence intervals, shortest length confidence intervals, Asymptotic Confidence Intervals based on CAN estimators, Variance stabilizing transformations (VST), confidence interval based on VST, Asymptotic Confidence regions.

(12L+3T)

**Unit 4:** Likelihood ratio test (LRT) and its asymptotic distribution, Wald test, Rao's Score test, Pearson Chisquare test of goodness of fit, Bartlett's test for homogeneity of variances. Large sample tests based on VST. Consistent test, comparison of tests: asymptotic relative efficiency of tests (Pitman and Bahadur efficiency). Performance evaluation (based on simulation) of asymptotic tests and confidence intervals.

(12L+3T)

- 1. Kale, B. K., & Muralidharan, K. (2015). Parametric inference: An introduction. Alpha Science International Limited.
- 2. Dudewicz, E. J. and Mishra, S. N. (1988). Modern Mathematical Statistics, John Wiley & Sons.
- 3. Ferguson, T. S. (2014). Mathematical statistics: A decision theoretic approach. Academic press.
- 4. Gibbons, J.D., & Chakraborti, S. (2010). Nonparametric Statistical Inference (5th ed.). Chapman and Hall/CRC.
- 5. Lehman, E. L. (1987). Theory of testing of hypotheses. Students Edition.
- 6. Randles, R. H., & Wolfe, D. A. (1979). Introduction to the theory of nonparametric statistics. John Wiley.
- 7. Rohatgi, V. K., & Saleh, A. M. E. (2015). An introduction to probability and statistics. John Wiley & Sons.
- 8. Zacks, S. (1971). Theory of Statistical Inference, John Wiley & Sons, New York.

## Title of Course: LINEAR MODELS AND REGRESSION ANALYSIS

#### Course Code: MSU0325MML905H2

#### Total Credits: 04

#### **Course outcomes:**

Upon successful completion of this course, a student will be able to:

- i) Understand the concept of general linear model and associated inferential procedures.
- ii) Understand and develop multiple linear regression models
- iii) Identify the problems in developing multiple linear regression models and apply remedies.
- iv) Understand generalized linear models and apply them for analyzing real data.

**Unit 1:** General linear model: definition, assumptions, concept of estimability, least squares estimation, BLUE, estimation space, error space, Gauss Markov theorem, variances and covariances of BLUEs, Distribution of quadratic forms for normal variables: related theorems(without proof), Tests of hypotheses in general linear models. Description of the ANOVA and linear regression models as the particular cases of the general linear model.

(12L+3T)

**Unit 2:** Multiple linear regression model, Least squares estimates (LSE) of parameters, Properties of LSE, Hypothesis testing, confidence and prediction intervals, General linear hypothesis testing, Model adequacy checking, Dummy variables and their use in regression analysis. Transformations to correct model inadequacies: VST and Box-Cox power transformation.

(12L+3T)

**Unit 3:** Multicollinearity: Consequences, detection and remedies, ridge regression. Autocorrelation: sources, consequences, detection (Durbin-Watson test) and remedies. Parameter estimation using Cochrane-Orcutt method. Variable Selection Procedures: R- square, adjusted R-square, Mallows' Cp, forward, backward and stepwise selection methods, AIC, BIC. Robust Regression: need for robust regression, M-estimators, properties of robust estimators: breakdown and efficiency. Asymptotic distribution of M-estimator (Statement only).

(12L+3T)

**Unit 4:** Generalized linear models: concept of generalized linear model, Link function, ML estimation, large sample tests about parameters, goodness of fit, analysis of deviance. Residual analysis, types of residuals: raw, Pearson, deviance, Anscombe, quantile; residual plots. Variable selection: AIC and BIC. Logistic regression: logit, probit and cloglog models for dichotomous data, ML estimation, Odds ratio and its interpretation, hypothesis tests about model parameters. Hosmer-Lemeshow test, multilevel logistic regression, Logistic regression for Nominal response. Poisson regression.

(12L+3T)

- 1. Birkes, D., & Dodge, Y. (2011). Alternative methods of regression. John Wiley & Sons.
- 2. Cook, R. D., & Weisberg, S. (1982). Residuals and influence in regression. New York: Chapman and Hall.
- 3. Draper, N. R., & Smith, H. (1998). Applied regression analysis. John Wiley & Sons.
- 4. Huber, P.J. and Ronchetti, E.M (2011) Robust Statistics, Wiley, 2nd Edition.
- 5. Kutner, M. H., Nachtsheim, C. J., Neter, J., & Wasserman, W. (2004). Applied linear regression models. New York: McGraw-Hill/Irwin.
- 6. Montgomery, D. C., Peck, E. A., & Vining, G. G. (2021). Introduction to linear regression analysis. 5th Ed. John Wiley & Sons.
- 7. Seber, G.A., Wild, C.J. (2003). Non linear Regression, Wiley.
- 8. Weisberg, S. (1985). Applied Linear Regression, John Wiley & Sons. New York.

#### **Title of Course:** STATISTICAL PROGRAMMING USING PYTHON **Course Code:** MSU0325MML905H3 **Total Credits:** 02 **Course outcomes:**

Upon successful completion of this course, a student will be able to:

- i) Develop programs in Python.
- ii) Perform data organization, data manipulation, statistical and mathematical computations, and data analysis using Python.

**Unit 1:** Introduction, installation, keywords, identifiers: variables, constants, literals; comments, Operators, statements and expressions, data types with methods: numbers, string, lists, tuple, dictionary, set; indexing and slicing of each data type, data type conversion, built-in functions, control statements and loops, list comprehensions, user defined functions, anonymous/lambda function, local and global variables, modules: math, stat, random;creating own modules.

(12L+3T)

**Unit 2:** Concept of library and its working, Data storage, manipulation, visualization and analysis using the libraries: Numpy, Pandas, Scipy, statsmodels, Matplotlip, Seaborn, Regular Expressions (RegEx), Ski-kit learn.

(12L+3T)

- 1. Gowrishankar, S., &Veena, A. (2018). Introduction to Python programming. CRC Press.
- 2. Guttag, J. V. (2021). Introduction to Computation and Programming Using Python: With Application to Computational Modeling and Understanding Data. Mit Press.
- 3. Haslwanter, T. (2016). An Introduction to Statistics with Python. With Applications in the Life Sciences. Switzerland: Springer International Publishing.
- 4. Nelli, F. (2018). Python data analytics with Pandas, NumPy, and Matplotlib.
- 5. Unpingco, J. (2016). Python for probability, statistics, and machine learning (Vol. 1). Springer International Publishing.
- 6. VanderPlas, J. (2016). Python data science handbook: Essential tools for working with data. " O'Reilly Media, Inc.".
- 7. URLs:
  - <u>https://scikit-learn.org/stable/</u>
  - <u>https://numpy.org/</u>
  - <u>https://scipy.org/</u>
  - <u>https://www.statsmodels.org/stable/index.html</u>
  - <u>https://matplotlib.org/</u>
  - <u>https://pandas.pydata.org/</u>

#### Title of Course: ADVANCED DATA STRUCTURE WITH C++ Course Code: MSU0325MEL905H1 Total Credits: 04 Course outcomes:

Upon successful completion of this course, the student will be able to:

- i) Write, compile, and execute programs in C++ and develop code in C++ by identifying the appropriate features of object oriented programming to solve statistical problems.
- ii) Explain the concept of data structures, choose appropriate data structure for a specific problem and implement linear data structures such as stacks, queues, linked lists
- iii) Implement tree data structure
- iv) Implement graph data structure and search data structures such as hashing

**Unit 1:** C++ programming basics. Data types, Variables, Statements, Expressions, Control structures, Looping, Functions, Arrays, Pointers. Object oriented programming: Concept of OOP, class and objects, inheritance, polymorphism (function and operator overloading).

(12 L + 3 T)

**Unit 2:** Data Structures: definitions, operations, implementations and applications of basic data structures. Stack, Applications of Stack, Queue, Priority Queue, circular queue Applications of queue, Linked lists, doubly linked list, circular list, dynamic memory allocation, implementation of linked list, further operations, implementation of sparse matrices.

(12 L + 3 T)

**Unit 3:** Trees, binary trees, binary search trees, operations on binary search tree, applications of binary trees, threaded binary trees. General trees, using binary trees to represent general trees. AVL tree, operations on AVL tree. 2-3 trees, operations on 2-3 tree. Multi-way search tress, B-trees, B-tree indexing, operations on B trees. Huffman coding.

(12 L + 3 T)

**Unit 4:** Graphs, representation, operations on graph, Applications of graph: shortest path problem, Dijkstra's algorithm, topological ordering, minimum spanning tree, DFS and BFS spanning tree, Kruskal's algorithm. Tables, Hash tables: hashing techniques, collision resolution techniques, closed hashing, open hashing.

(12 L + 3 T)

- 1. Decker, R., & Hirshfield, S. (1995). *Object Concept: An Introduction to ComputerProgramming Using C++*. International Thomson Computer Press.
- 2. Kanetkar Y. (2003). *Data Structures through C++*. BPB Publications.
- 3. Kruse, R., & Tondo, C. L. (2007). *Data structures and program design in C*. PearsonEducation India.
- 4. Samanta, D. (2001). *Classic data structures*. Prentice Hall India.
- 5. Sartaj, S. (1998). Data structures, algorithms, and applications in C++. McGraw-HillBoston, MA, USA
- 6. Savitch, W. J., & Savitch, W. (2003). *Problem solving with C++: The object ofprogramming*. Addison Wesley.
- 7. Stanley, B., & LIPPMAN, L. (2019). *C++ PRIMER*. Addison-Wesley.
- 8. Weiss, M. A. (2014). *Data structures and algorithm analysis in C++*. Pearson.

## **Title of Course:** PRACTICAL II **Course Code:** MSU0325MMP905H4 **Total Credits:** 04

#### Course outcomes:

Upon successful completion of this course, the student will be able to:

- i) Test hypothesis about the parameters and provide interval estimates involved in random experiments based on random sample.
- ii) Perform statistical analysis, such as estimation, hypothesis testing, and analysis of variance, under generalized linear models
- iii) Fit linear regression model or Generalized Linear Regression Models to the data, perform diagnostic analysis and apply rectifying measures to overcome the problem of Multicollinearity, auto-correlation, outliers and non-linearity.
- iv) Perform mathematical/statistical computations, statistical data analysis using built-in functions in Python and develop programs for various tasks.

#### **Practical List:**

- 1. MP, UMP, and UMPU Tests
- 2. Tests based on Hotelling's T<sup>2</sup> statistic
- 3. Confidence Intervals
- 4. Likelihood ratio tests
- 5. Linear Estimation: Estimation and Hypothesis testing
- 6. Performance evaluations of confidence intervals and tests through simulation.
- 7. Multiple linear regression
- 8. Variable selection in regression
- 9. Dealing with multicollinearity, autocorrelation and outliers
- 10. Logistic Regression
- 11. Poison regression
- 12. Monte Carlo Simulation of Regression Models
- 13. Python programming-I
- 14. Python programming-II
- 15. Python Programming-III
- 14-20. Based on elective paper

## 9. Scheme of Teaching

- Theory courses: One hour per week per credit
- Practical courses: Three hours per week per credit
- Project: Three hours per week per credit

## **10. Examination Pattern**

- Theory: 20% marks for internal examination and 80% marks for university examination
- Practical: 100% marks for internal evaluation
- On Job Training: To be decided by BoS
- Field Project: To be decided by BoS
- Research Methodology: 20% marks for internal examination and 80% marks for university examination

## 11. Nature of Question Paper and Scheme of Marking

#### **Theory Examination:**

- Nature of the theory question papers (4 credits):
  - a) There shall be 7 questions each carrying 16 marks.
  - b) Question No.1 is compulsory. It consists of 8 questions for 2 marks each.
  - c) Students have to attempt any 4 questions from question No. 2 to 7.
  - d) Question No. 2 to 6 shall contain 2 to 4 sub-questions.
  - e) Question No. 7 shall contain 4 short note type questions, each carrying 4 marks.

#### • Nature of the theory question papers (2 credits):

- a) There shall be 4 questions.
- b) Question No.1 is compulsory. It consists of 4 questions for 2 marks each.
- c) Question No. 2 to 4 shall be of 16 marks each.
- d) Students have to attempt any 2 questions from question No. 2 to 4.
- e) Question No. 2 to 4 shall contain 2 to 4 sub-questions.

#### **Practical Examination:**

Component	Max marks
Practical examination:	60
Examination will be of 3 hour duration. There shall be 8 questions each of 12 marks, of which a student has to attempt any 5 questions.	
Day-to-day practical performance and journal	20
Viva: Viva will be based on all practical's	20

# 1. Equivalence of courses

		Old Course	Equivalent Course				
Sem No.	Course Code	Title of Old Course	Cre dit	Course Code	Title of New Course		
Ι	CC-101	Fundamentals of Computer Programming	4	ME12	Fundamentals of Computer Programming	4	
Ι	CC-102	Linear Algebra	4	ME13	Linear Algebra (M. Sc. Statistics)	4	
Ι	CC-103	Distribution Theory	4	MM11	Distribution Theory	4	
Ι	CC-104	Estimation Theory	4	MM12	Estimation Theory	4	
Ι	CC-105	Statistical Computing	4	RM	Research Methodology in Statistics	4	
Π	CC-201	Advanced Data Structure With C++	4	ME21	Advanced Data Structure With C++	4	
Π	CC-202	Theory of Testing of Hypothesis	4	MM21	Theory of Testing of Hypothesis	4	
Π	CC-203	Linear Models and Regression Analysis	4	MM22	Linear Models and Regression Analysis	4	
ΙΙ	CC-204	Design and Analysis of Experiments	4	ME31	Design and Analysis of Experiments	4	
II	CC-205	Sampling Theory and Official Statistics	4	No equivalence can be given for these courses in the new syllabus as per NEP 2020.			

M. Sc. Part I (Semester I and II)

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